

A. Division: ACADEMIC Date: October, 1985

B. Department: SCIENCE AND MATHEMATICS New Course:

Revision of Course Information Form:

Dated: May, 1984

C. MAT 450 D. Quantitative Methods E. 3

Subject & Course No. Descriptive Title Semester Credits

F. Calendar Description:

Applications of mathematics to business and economics, with emphasis on non-linear models. Includes multivariate functions, probability theory, transformations of data, marginal analysis, Lagrange multipliers, utility theory, non-linear programming, method of least squares, and differential equations. Some topics are optional and may be omitted or included dependent on class interest.

Summary of Revisions:
(Enter date and Section Revised)
e.g. 1982-08-25
Section C,E,F, and R.

1985-09-18

Form Updated

Sections N, Q, R

Sections O & P revised to reflect changes at UBC and SFU

G. Type of Instruction:	Hours Per Week / Per Semester	H. Course Prerequisites:
	Lecture <u>4</u> Hrs.	MAT 250 or MAT 120/220
	Laboratory _____ Hrs.	I. Course Corequisites:
	Seminar _____ Hrs.	Macro/Micro economics helpful
	Clinical Experience _____ Hrs.	J. Courses for which this Course is a Pre-requisite:
	Field Experience _____ Hrs.	NONE
	Practicum _____ Hrs.	K. Maximum Class Size:
	Shop _____ Hrs.	35
Studio _____ Hrs.		
Student Directed Learning _____ Hrs.		
Other (Specify) _____ Hrs.		
Total <u>4</u> Hrs.		

L. College Credit Transfer <input checked="" type="checkbox"/>	M. Transfer Credit: Requested <input type="checkbox"/>
College Credit Non-Transfer <input type="checkbox"/>	Granted <input checked="" type="checkbox"/>
Non-Credit <input type="checkbox"/>	(Specify Course Equivalents or Unassigned Credit as Appropriate)
	U.B.C. MAT 450 - Math 141 (1.5)
	S.F.U. MAT 450 - Math 158 (3)
	U. Vic. {MAT 350/450 - Math 240(3)}
	Other {MAT 450 - Math (200 level) (1.5)}

John Atwell
Course Designer(s)

S.M. Wilson
Divisional Dean

D. Dellabattia
Acting Registrar

[Signature]
Director / Chairperson

 N. Textbooks and Materials to be Purchased by Students (Use Bibliographic Form):

**Goldstein, Lay and Schneider - Calculus and Its Applications, 3rd Ed.
Prentice-Hall Publishing**

 Complete Form with Entries Under the Following Headings: O. Course Objectives; P. Course Content;
Q. Method of Instruction; R. Course Evaluation

 O. Course Objective & P. Course Content

This is the old MAT 450 starting from a somewhat more elementary point because it includes some methods of integration and probability topics formerly included in MAT 250. Additionally, multiple integrals and periodic functions will be added. Less time will be required reviewing some basic ideas because this course should follow directly on the heels of MAT 250, rather than their being separated by at least a semester.

1. Methods of integration

Parts

Discounting and compounding income streams

Partial fractions

The logistic

Improper integrals

Integrals of negative powers to infinity

2. Probability distributions

Normalizing relative density functions

Expectation, variance, and standard deviation

Testing hypotheses concerning mean by sampling

Random variables with infinite domains

The exponential and normal probability densities

Use of normal distribution tables

3. Cyclic behaviour and the sine and cosine

Need for cyclic functions

Mechanical generation of sine and cosine waves

 Graphs of $A \sin(a+bt)$, $A \cos(a+bt)$

Compounding wave forms

Derivative of sine and cosine

Equation of simple harmonic motion

4. Functions of several variables

Production and utility functions

 Representation of $z = f(x,y)$ in 3-dimensions

Contours and cross-sections
 Isoquants, indifference curves and production frontiers
 Slopes in directions of axes and partial derivatives
 Marginal concepts
 Total differentials and directional derivative
 Changes in total cost, utility
 Marginal rates of substitution
 Elasticity concepts
 CES and Cobb-Douglas functions
 cross elasticity of demand
 elasticity of substitution
 Locating extremes
 First derivative conditions
 Saddle points
 Second derivative test
 Optimizing with constraint
 by elimination of variables
 by Lagrange multipliers
 "Design" problems with and without constraint
 Optimizing utility subject to budget
 The Bowley-box

5. Multiple integrals

Iterated integrals over rectangles
 Integrals over $\{(x,y) \mid g(x) \leq y \leq f(x), a \leq x \leq b\}$

Topics 5,7,8,9 as time permits and interest dictates.

6. The method of least squares

Justification for least squares
 Dangers inherent
 Fitting $y=ax+b$, $y=ax$, $y=b$
 Fitting $y=ax^2+bx+c$, etc.
 Fitting $z=ax+by+c$, etc.
 Fitting $y=a^{bx}$, $y=Ae^{bx}$, $y=Ax^b$
 Applications to growth, learning, imputing costs

7. Models employing differential equations

Domar growth model ($Y=aK$, $I=f(Y)$)
 Market equilibrium models with inventories
 $dp/dt = a(D-S)$, $S=f(p)$, $D=g(p)$
 $dp/dt = a(D-S)$, $dS/dt = f(p)$, $D-g(p)$

8. Steepest ascent methods

"small step" (of Gauss's method)
 "optimal step"

9. Homogeneous functions

Returns to scale
 Euler's theorem
 Clark-Wicksteed theorem

Q. Methods of Instruction

Classes meet four hours per week. Abstractions will be developed from specific problems; a significant component of lectures will consequently be solving problems.

Students should expect regular problem assignments that will exercise and expand upon the lecture's topics.

R. Course Evaluation

The final grade assigned for the course will be based on the following:

1. Classroom tests 70%
2. Final Examination 30%

Notes

- i. There will be three or more in-class tests spread over the semester.
- ii. At the discretion of the instructor the percentage for the classroom tests may be reduced and replaced by problem assignments. If problems are assigned for marking the number of tests may be reduced to two. The maximum to be awarded for assignments is 20%
- iii. A comprehensive, three hour exam will be held at the end of the semester.

In the event that the student's letter grade on the final exam is higher than the normally calculated grade, the final grade will be increased one level (i.e. if the term average indicates a C grade and the score on the final exam is an A or B, then a B grade will be awarded).

The calendar states that a C grade is based on consistently average work. Those students who do poorly on the final exam (i.e. the final exam score is well below the average), may be awarded no more than a P grade even though their term average, as normally calculated, indicates a C grade.